# Quadratic Terms based Point-to-Surface 3D Representation for Deep Learning of Point Cloud

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Abstract-In this paper, we introduce a novel point-to-surface representation for 3D point cloud learning. Unlike the previous methods that mainly adopt voxel, mesh, or point coordinates, we propose to tackle this problem from a new perspective: learn a set of quadratic terms based static and global reference surfaces to describe 3D shapes, such that the coordinates of a 3D point (x, y, z) can be extended to quadratic terms (xy, xz, yz, ...) and transformed to the relationship between the local point and the global reference surfaces. Then, the static surfaces are changed into dynamic surfaces by adaptive contribution weighting to improve the descriptive capability. Towards this end, we propose our point-to-surface representation, a new representation for 3D point cloud learning that has not been attempted before, which can assemble local and global geometric information effectively by building connections between the point cloud and the learned reference surfaces. Given 3D points, we show how the reference surfaces are constructed, and how they are inserted into the 3D learning pipeline for different tasks. The experimental results confirm the effectiveness of our new representation, which has outperformed the state-of-the-art methods on the tasks of 3D classification and segmentation.

*Index Terms*—3D representation, Point cloud segmentation, Point cloud classification, 3D deep learning.

#### I. INTRODUCTION

THREE-DIMENSIONAL deep learning has attracted extensive attentions in recent years, including but not limited to, 3D classification [1], [2], 3D segmentation [3], [4], shape completion [5], object detection [6], and 3D scene understanding [7]. The learning of 3D point cloud is still facing many challenges, due to the difficulties regarding the inference of the underlying shapes from irregular point clouds. Many works have been proposed to tackle this problem, from volumetric representation that converts 3D shape into 3D grids for 3D CNN [8], [9], to multi-view image representation [10], [11] and then to directly point cloud processing that feeds the points to the network inputs [1], [12], [3].

Qi *et al.* [1] proposed a point-wise feature learning network, PointNet, which consumes the points directly for 3D learning. However, though impressive, this design ignores the local

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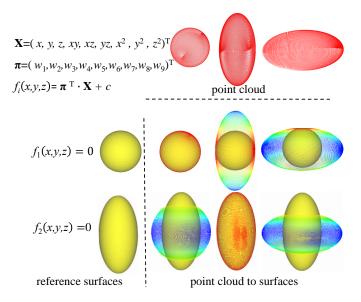


Fig. 1. The shape of a point cloud can be described by comparing with reference surfaces. In order to represent the local and global geometrical information for a point  $\mathbf{p}$ , the coordinates are extended to high-order and weighted by every different surface function coefficients to obtain function values. These values include local and global features. Then, they are used for point representation.

structures that is important for 3D tasks [13]. Later, the PointNet++ [12] is proposed to use hierarchical networks to learn local features with increased contextual scales. In order to further extract topological information of local point clouds, Wang *et al.* [14] presented a Dynamic Graph Convolutional Neural Network (DGCNN) with Edge-conv. Then, based on hierarchical CNN like PointNet++ [12], Liu *et al.* [3] encoded the geometric priors of neighbors for high-level relation learning. However, these methods are limited to the relationship between point coordinates when extracting the local geometric features.

In general, there are three main challenges regarding the point cloud learning. First, how to capture good local and global features due to the disorder of point cloud. Second, how to represent effective geometric information of the underlying shape by giving the point coordinates. Third, how to calculate point cloud features in a simple and effective way. These challenges are open problems that are under exploration mainly by modifying the network architectures and designs [12], [14], [3]. In this work, we tackle the issue from a new perspective, where we modify the representation at the beginning.

To this end, we propose our quadratic terms based point-to-

This work was supported by the National Natural Science Foundation of China under Grants 62071097, 61872067, and U20A20184. (*Corresponding author: Guanghui Liu*).

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surface 3D representation considering both the point and the geometric surface simultaneously. Fig. 1 shows some simple examples. The surfaces to the left of the dashed line are defined as the reference surfaces. Each surface can be expressed as f(x, y, z) = 0. The function f(x, y, z) is defined as a surface function, which is composed of the first and second order terms  $(x, y, z, xy, xz, yz, x^2, y^2, z^2)$  and a constant. Fig. 1 gives three point clouds with simple shape, a sphere and two ellipsoids. In order to describe the point cloud locally and globally, we use the point cloud of the entire dataset to learn the global reference surface. Then, all points in the point cloud are taken as inputs of the global surface function f(x, y, z). Through this operation, if a point  $\mathbf{p} = (x, y, z)$  is on the surface, then  $f(\mathbf{p}) = 0$ . If all the function values of local points are equal to zero, then the surface f(x, y, z) = 0 is part of the input model around these local points. Otherwise, the value of f(x, y, z) is not equal to zero but depends on the distance. As shown in Fig. 1, when the point cloud coincides with the surface, it appears red. If the point is moving away from the surface, it appears in a gradient of other colors. Therefore, the function values of local points reflect the local features. Moreover, the surface f(x, y, z) = 0 is learned through the entire point clouds, it is a global shape, so the surface function value  $f(\mathbf{p})$  of point  $\mathbf{p} = (x, y, z)$  can also indicate the relative position relationship between the local point and the global surface. Therefore, both local and global information is implicit in this representation.

In this paper, the reference surfaces are determined by learning the coefficients for the terms of f(x, y, z), as shown in Fig. 1 ( $w_1 \sim w_9$ , c). These coefficients do not require special supervised learning. They can be easily learned within only one convolution layer in the specific 3D tasks training. In this process, we can learn  $N_f$  reference surfaces at one time. Then, every point in the point cloud can be fed into the  $N_f$  surface functions, resulting  $N_f$  point-wise representation as the input of the subsequent networks for specific 3D analysis. After training, these coefficients are stored in the checkpoint. For the testing data, however, these surfaces are static, which limits the richness and description capability of the reference surfaces. We prefer dynamic surfaces to describe different shapes accordingly. Therefore, we utilize the initial representation to learn the contribution weights of each surface to each point and weight the initial representation to implement the dynamic representation.

In summary, our main contributions are as follows:

- We propose a quadratic terms based point-to-surface representation for point cloud learning, which addresses the point cloud representation from a new perspective.
- We propose a dynamic representation based on the adaptive contribution weighting to improve the descriptive capability of the point-to-surface representation.
- The new representation can effectively grasp local and global features, facilitating the point cloud analysis.
- The proposed point-to-surface module is plug-and-play, which can be inserted into various 3D pipelines seamlessly, creating new state-of-the-art performances, validated on 3D classification and segmentation tasks.

## II. RELATED WORKS

## A. Depth Image Representation

Compared to point cloud, depth image is orderly and regular. Depth image can be easily obtained by stereo disparity estimation [15], monocular depth estimation [16] and some depth camera such as Kinect [17]. Therefore, depth-based 3D tasks are widely concerned. For example, Soltam et al. [18] proposed to synthesize 3D shapes via multi-view depth maps with generative network. Ren et al. [7] proposed monocular depth estimation for 3D indoor and outdoor scene understanding. Some works [19], [20] studied the pose estimation using depth image directly. In contrast, Chen et al. [21] proposed a method that converts the depth image into point cloud with the intrinsic parameters of the camera. Then, they reconstructed the encoder of the SO-Net [22] to estimate the hand pose using point cloud. Yavartanoo et al. [23] projected the 3D model to multiple 2.5D depth maps for learning representations of 3D objects with a Stereographic Projection Neural Network (SPNet). However, depth-based methods are limited by the accuracy of depth estimation.

## B. Mesh Representation

Mesh is very difficult to extract shape features due to the complexity and irregularity. Han et al. [24] proposed mesh convolutional restricted Boltzmann machines to simultaneously learn local and global features from the mesh data. For 3D mesh segmentation, Le et al. [25] rendered the mesh model into multiple views to learn edges with CNN. Then, these edges were unprojected back to 3D mesh for mesh segmentation. Although this method avoids the complexity and irregularity of mesh data through multi-view images, the original mesh information is still not used for feature extraction. Recently, Feng et al. [26] proposed a mesh neural network (MeshNet) for 3D shape representation using original mesh data. They regarded the triangular face as the unit. So the disorder problem is solved by per-face processing. Then, the geometrical information of triangular face are calculated for 3D task learning. The experiments demonstrate the effectiveness of MeshNet. Taha et al. [27] defined an inverse mapping between the 3D mesh and the 2D texture image. They mapped the 3D mesh features to 2D images for 3D shape representation. The method has been applied to facial expression and action recognition.

# C. Multi-view Representation

Some researches proposed to render the 3D shape to multiview images for 3D classification [28] and shape retrieval [29], [30]. Gadelha *et al.* [31] proposed to utilize multi-view images to restore 3D shape with projective generative adversarial networks. Considering the similarities and differences between multi-view images, Feng *et al.* [11] proposed a group-view CNN network for 3D shape recognition. Different from the view-wise feature extraction, Yu *et al.* [10] aggregated the multi-view local features by bilinear pooling. Then, they harmonized these bilinear feature components for 3D representation. Huang *et al.* [2] proposed to render 3D object as multiview images to learn a disentangled representation for 3D classification. These methods convert disordered 3D data into ordered 2D images. Then, the mature 2D scene understanding techniques are applied to 3D understanding.

# D. Volumetric Grids Representation

Volumetric grids representation is another commonly used 3D representation. Wu et al. [8] first proposed ShapeNet to represent a geometric 3D shape as a probability distribution on volumetric grid. Following the ShapeNet [8], Sharma et al. [9] presented an unsupervised learning volumetric representation for denoising, shape completion and classification. Wu et al. [32] proposed 3D generative adversarial network based on volumetric convolutional networks for 3D shapes generation. Xu et al. [33] extended the voxel hashing to point cloud voxel representation. They used an efficient multi-scale voxel representation for collision detection in augmented reality scene. In order to extract the point-wise feature, Zhou and Tuzel [34] proposed VoxelNet to partition the space into voxels and aggregate the point-wise feature in each voxel to shape information as voxel-wise feature. Finally, the voxel-wise feature can be used for object detection. Le and Duan [35] proposed the PointGrid to integrate point and grid for preserving the original coordinates. Signed Distance Function (SDF) is also commonly used for voxel-based representation [36], [37]. SDF values are calculated for each voxel. Then the zero iso-surface represents the shape information that can be used for shape completion and 3D reconstruction. However, these voxel-based methods require a lot of memory and computation. Moreover, the representation power is limited by voxel resolution.

# E. Point-wise Representation

Recently, Qi et al. [1] proposed the PointNet to directly extract the point-wise features. Then a symmetric function was used for extracting the global feature. However, PointNet does not capture local structures. To address this problem, Qi et al. [12] also proposed a hierarchical neural network to extract the local features of multi-scale neighborhood points. Achlioptas et al. [38] proposed a learning representation method based on encoder and decoder network for transforming point into a latent space. Wang et al. [39] proposed a parametric continuous convolution to extract points features. Considering the relationship between neighborhood points, Wang et al. [14] proposed Dynamic Graph CNN (DGCNN) to expand the receptive field with dynamic graph updates. Inspired by DGCNN, Wang and Solomon [40] utilized DGCNN to align two point clouds. Liu et al. [3] proposed a Relation-Shape Convolutional Neural Network (RSCNN) for feature learning from the relation between neighbor points.

However, when extracting shape features, these methods only use the coordinates to extract the relationship between points, instead of analyzing the features between the point and surface. Therefore, in this paper, we propose to use the quadratic terms of the point coordinates and the learned reference surfaces to construct a new point-to-surface representation without loss of information, which is different from any of the previous 3D representations mentioned above.

## III. METHOD

In this section, quadratic terms based point-to-surface representation is first formulated and proposed (Sec. III-A). In order to enhance the description capability of local characteristics, an adaptive contribution weighting optimization is proposed (Sec. III-B). Then, we introduce our point-to-surface module (Sec. III-C). After that, we apply the point-to-surface module to the previous network structures for classification and segmentation (Sec. III-D). Finally, we introduce the detailed training process (Sec. III-E).

# A. Quadratic Terms based Point-to-Surface Representation

From the point of view of human perception, when we perceive an object, we usually look at the appearance of the object and compare it with our reference models accumulated through our past experience. Then, we can determine if the object has been seen. If so, what is it? Based on this understanding, this paper proposes to use the reference surface to describe the 3D object in the form of point cloud. In the real world, no matter from which angle we look at an object, we cannot see the whole picture of it. This is because objects have front and back views in any perspective. Therefore, if a function can represent a 3D shape, the function must be quadratic. For example, if the shape is a sphere, the surface can be expressed as:

$$x^2 + y^2 + z^2 - r = 0, (1)$$

where r is the radius of the sphere. For a ruled quadrics surface [41], the equation is

$$xy - z = 0. (2)$$

More generally, these quadratic terms based surfaces can be formulated as:

$$\mathbf{X} = (x, y, z, xy, xz, yz, x^2, y^2, z^2)^T, 
\pi = (w_1, w_2, w_3, w_4, w_5, w_6, w_7, w_8, w_9)^T, 
f(x, y, z) = \pi^T \cdot \mathbf{X} + c = 0,$$
(3)

where the vector **X** represents the terms of the function f(x, y, z), defined as quadratic terms, the notation  $\pi$  represents the coefficients of these terms, and c is a constant. Here, we use F(x, y, z) = 0 to represent a set of reference surfaces  $f_i(x, y, z) = 0$  with the number of  $N_f$ ,  $i \in [1, N_f]$ . If we represent the reference surface as a function f(x, y, z), the value of the function f(x, y, z) is related to the distance between the point and the surface. For example, if  $f(x_i, y_i, z_i) = 0$ , then the point  $\mathbf{p}_i = (x_i, y_i, z_i)$  is on the surface; otherwise, it is not on the surface. The function f(x, y, z) corresponding to a continuous surface is also continuous, so the value of f(x, y, z) represents the relationship between a 3D point  $\mathbf{p} = (x, y, z)$  and the surface f(x, y, z) = 0. For the surface function set F(x, y, z), all the function values form a new representation, formulated as:

$$\mathbf{A}_{N_f \times 10} \bar{\mathbf{X}} = \mathbf{R},\tag{4}$$

where the matrix  $\mathbf{A}_{N_f \times 10}$  is made up of  $N_f$  surface parameters. The vector  $\mathbf{X}$  is the homogeneous expression of  $\mathbf{X}$ . The vector  $\mathbf{R}$  is the new representation with the size of

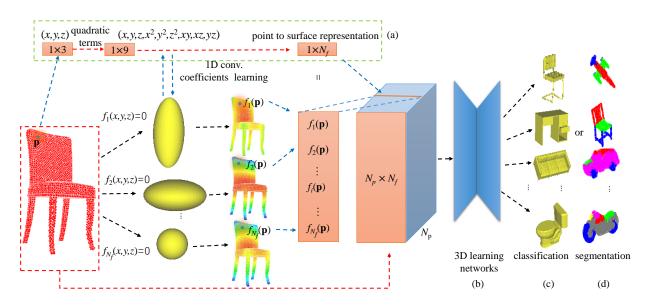


Fig. 2. The pipeline of point-to-surface representation. The quadratic terms are calculated by the point coordinates. Then a 1D convolution is used for learning the function coefficients. For a point  $\mathbf{p}$ , feeding quadratic terms into convolution layer can obtain its point-wise representation with the size of  $1 \times N_f$ . For a point cloud with  $N_p$  points, the surface functions yield a  $N_p \times N_f$  feature. Then, this feature is inserted into 3D learning networks for point cloud analysis.

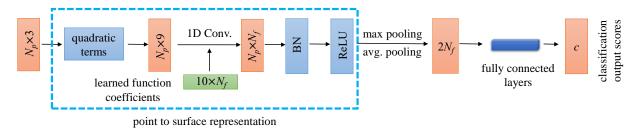


Fig. 3. The classification baseline based on the proposed point-to-surface representation. The baseline first calculates the quadratic terms by giving point coordinates. Then, the quadratic terms are transformed to point-to-surface representation through a 1D convolution layer, a batch normalization (BN) layer and a ReLU layer successively. Finally, the classification scores are obtained by the following pooling layers and fully connected layers.

 $N_f$ . The 9 quadratic terms are considered as 9 unknowns. If the rank of matrix  $\mathbf{A}_{N_f \times 10}$  is equal to 9, Equation (4) has a unique solution. Assuming that these surface functions are linearly uncorrelated, if the number of surface functions is greater than 9, i.e.,  $N_f \geq 9$ , the original unique point coordinates can be solved with the new representation  $\mathbf{R}$  and the surface parameters  $\mathbf{A}_{N_f \times 10}$ . Therefore,  $N_f \geq 9$  is a sufficient condition for no-loss representation.

Fig. 2 shows our pipeline. Given a 3D point  $\mathbf{p} = (x, y, z)$ , the quadratic terms can be directly calculated by the coordinates of points while the coefficients of the terms need to be estimated. Here, a surface function contains 9 coefficient weights  $(w_1 \sim w_9)$  and one bias c as unknowns to be estimated. To estimate a surface function  $f_i(x, y, z)$ , we use the entire point clouds from dataset for the estimation. The coefficients estimation is implemented through the 3D tasks training. Instead of estimate a set of  $N_f$  functions all at once. As such, we estimate  $N_f \times 10$  unknowns for all surface functions. After  $N_f$  surfaces being learned, a point  $\mathbf{p}$  can be calculated for its new features, yielding a feature of size  $1 \times N_f$  (Fig. 2(a)). For a point cloud with  $N_p$  points, yielding a feature of size  $N_f$ , which are inserted into 3D learning networks

for subsequent tasks (Fig. 2(b)), such as classification and segmentation (Fig. 2(c) and (d)). Based on this pipeline, we define a classification baseline as shown in Fig. 3. The baseline first calculates the new representation with a 1D convolution layer, a Batch Normalization (BN) layer and a ReLU layer. Then, the representation is fed into pooling layers and fully connected layers to get classification scores.

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# B. Adaptive Contribution Weighting

When the network training is finished, the learned global reference surfaces have been fixed. They are static for the testing data, which limits the richness and the descriptive capability of the reference surfaces for various shapes. To address this problem, we propose an adaptive contribution weighting optimization to weight the initial representation, equivalent to weighting the original reference surfaces. Then, we can use these dynamic reference surfaces to describe different shapes accordingly.

Specifically, we convert the initial point-to-surface representation into contribution weights through the convolution layers. This is because the initial point-to-surface function value is related to the distance from the point to the surface, implying the relationship between the point and the reference surface.

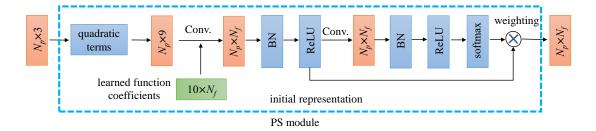


Fig. 4. The structure of PS module. The PS module first calculates the initial point-to-surface representations as the baseline. Then, the initial representations are used to calculate the contribution weights. Finally, the initial representations are weighted by the calculated weights to get the final point-to-surface representation.

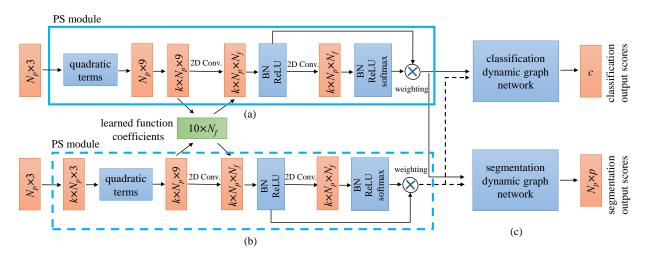


Fig. 5. The modified DGCNN [14] with the proposed point-to-surface representation for classification and segmentation. For classification, the input of the PS module is the original point cloud. While for segmentation, the input is the transformed point cloud with non-Euclidean coordinates. The nearest-neighbor searching can be based on point coordinates or features, so the PS module has two forms as shown in (a) and (b). ( $N_p$ : the number of the input points.  $N_f$ : the number of the reference surfaces. c: the number of the categories. p: the number of the segmentation parts.)

In addition, this information is different from each point for every surface, so this point-wise information can be used for adaptively learning the contribution of each reference surface to each point. The contribution learning model includes a convolution layer with the kernel size of 1, a BN layer, a ReLU layer and a softmax layer. The size of the learned contribution weights is the same as the initial representation. In this way, we use the learned weights to weight the initial representation to get the final point-to-surface representation. This method is equivalent to changing the static and global surfaces into dynamic global surfaces. Since the learned weights are different for each point, this dynamic representation can further enhance the local characteristics.

#### C. Point-to-Surface Module

To learn the reference surface functions, all point-wise quadratic terms are fed into a 1D convolution with the kernel size of 1. The weights and bias in 1D convolution are surface coefficients and constant. Therefore, the input channel of the 1D convolution is the number of function terms, i.e., 9. We estimate a set of  $N_f$  surface functions. Accordingly, the output channel of the 1D convolution is set to be  $N_f$ . Then, for a point **p**, the outputs of the 1D convolution are  $N_f$  values, corresponding to  $N_f$  surface function values. For a point cloud with  $N_p$  points, after 1D convolution, the initial representation is extracted based on the quadratic terms and reference surfaces, yielding a feature of size  $N_p \times N_f$ . Considering that f(x, y, z)may have a domain, to fit the boundary, an activation function is used for activating the output of the convolution.

For adaptive contribution weighting, the initial representation is fed into a new 1D convolution layer with the kernel size of 1. Both the input and output channels are set to  $N_f$ . Then a BN layer, a ReLU layer and a softmax layer are followed to get the contribution weights. Finally, the initial representation is weighted by these weights to get the final dynamic representation.

We call the above implementation a Point to Surface (PS) module as shown in Fig. 4. The input of the PS module is point cloud, and the output is the new representation. Note that, the PS module is plug-and-play, which can be inserted into the existing 3D learning pipelines seamlessly, where the reference surface function coefficients in the module are learned with its binding pipeline during the learning of specific 3D tasks. Different tasks with different pipelines may result in different surface function parameters for their own optimization.

#### D. 3D Classification and Segmentation

Extracting the local and global shape information of point cloud is important for 3D classification and segmentation.

This article has been accepted for publication in a future issue of this journal, but has not been fully edited. Content may change prior to final publication. Citation information: DOI 10.1109/TCSVT.2021.3095233, IEEE Transactions on Circuits and Systems for Video Technology



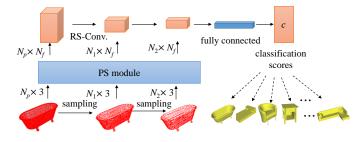


Fig. 6. The modified RSCNN [3] with the proposed point-to-surface representation for classification. Different from the original structure, the modified network no longer extracts the feature of point coordinates directly, but extracts the feature of the new representation obtained through PS module.

However, the traditional method extracts the point-wise feature solely based on point coordinates (x, y, z), which may underfitting for 3D surfaces. Here, we use our point-to-surface representation.

We plug our PS module into two representative networks for point cloud classification and segmentation. The two networks are dynamic graph network DGCNN [14] and RSCNN [3]. DGCNN [14] is based on dynamic graph structure for extracting topology information. RSCNN [3] inherits the Point-Net++ [12] hierarchical structure while learning the geometric information of the neighborhood at a high-level. The modified DGCNN is shown in Fig. 5. The classification and segmentation networks modified by RSCNN are shown in Fig. 6 and Fig. 7, respectively.

As for DGCNN [14] and RSCNN [3], they both extract k neighborhoods for each point as local geometrical information by k-nearest neighbors searching or ball-query searching. As shown in Fig. 5, if the neighborhood is obtained in feature space, we first calculate the quadratic terms. Then, these terms are used for neighbor searching (Fig. 5(a)). If the neighborhood is obtained by point coordinates, the quadratic terms calculation follows the neighbor searching (Fig. 5(b)). After the neighbor searching, we get a feature with the size of  $k \times N_p \times N_f$ . Therefore, the function coefficients should be learned by 2D convolution in PS modules.

In the modified DGCNN, the point cloud is first transformed into the point-to-surface representation with our PS module for the classification. For the segmentation, the PS module follows the spatial transformation. After PS module, the new representation is fed into the dynamic graph network (Fig. 5(c)) for classification and segmentation. For the details of DGCNN, please refer to [14]. The modified RSCNN for classification is shown in Fig. 6. The hierarchical architectures input different number of points. These point sets are first represented by our point-to-surface representation through a PS module as illustrated in Fig. 5(b). Then, this representation is used for classification features learning with RS-Conv. [3]. Finally, the fully connected layers follows the network to obtain the classification scores. The modified RSCNN for segmentation is shown in Fig. 7. Sampled multiple point sets are also fed into our PS module to get the new representation. Then, this representation is used for extracting local and global features through RS-Conv. [3] and skip connection. The features concatenate the category feature. This category feature

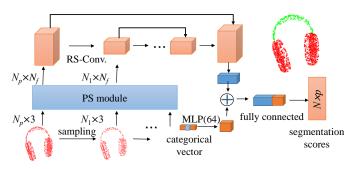


Fig. 7. The modified RSCNN [3] with the proposed point-to-surface representation for segmentation. Different from the original structure, the point Euclidean coordinates are first transformed to new representation through PS module for further feature extraction.

is obtained by extending the one-hot categorical vector with a MLP layer as the strategy in [14]. Finally, the concatenated features are used for learning the segmentation scores.

#### E. Implementation Details

The network is trained on a 1080 Ti GPU device. For the modified DGCNN, we use Stochastic Gradient Descent (SGD) optimizer to minimize the classification and segmentation loss function [14]. For the modified RSCNN, the optimizer is Adam. In classification experiments, the epoch is set to 400 for full convergence. When the input shape has 2,048 sampling points, the batch size is B = 8. While for 1,024 points input, the batch size is B = 16. In segmentation experiments, the epoch is set to 200 for full convergence. The batch size is set to B = 16. The number of the reference surface functions F(x, y, z) is set to 64. Our method is implemented by Pytorch. The modified networks are implemented based on the public codes of DGCNN [14] and RSCNN [3].

# **IV. EXPERIMENTS**

In this section, we first introduce the experimental datasets. Then, the baseline of our method is analyzed in terms of effectiveness, classification performance and complexity. Next, we evaluate the point-to-surface representation on 3D classification, part segmentation and semantic segmentation. After that, we analyze the proposed method through ablation study. Finally, we visualize the learned reference surfaces and the point-to-surface representation.

#### A. Experimental Datasets

We evaluate our method on popular 3D classification benchmark dataset, *i.e.* ModelNet10 (MN10) and ModelNet40 (MN40) [8]. Both datasets are CAD models. In the experiment, we sample 1,024 or 2,048 points uniformly. ModelNet40 dataset has 40 categories with 9,843 training samples and 2,468 testing samples. While ModelNet10 has 10 categories with 3,991 training samples and 908 testing samples. For shape part segmentation, we use the popular ShapeNet part benchmark [42] to evaluate our method. This dataset has 16 categories with 50 parts. In the experiment, 2,048 points are selected as inputs. For semantic segmentation, we use the popular ScanNet [43] benchmark for evaluation.

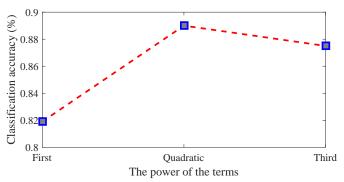


Fig. 8. The classification accuracy on different power of terms. The first and third order terms results are obtained by replacing the quadratic terms of the baseline model by the first and third order terms, respectively.

# B. Point to Surface Representation Evaluation

We first illustrate the effectiveness of our point-to-surface representation by comparing quadratic terms with the first and third order terms based on our baseline. Then, we extend our baseline with popular network structures such as DGCNN [14] and RSCNN [3] for 3D classification and shape part segmentation. Finally, we extend the PS module to FPConv [44] for semantic segmentation. The performance of our method is analyzed by comparing the results that before and after modification.

1) Analysis of Baseline: We first validate effectiveness of the proposed quadratic terms based baseline as shown in Fig. 3. We compare them with the first and third order terms. The first order terms include x, y and z. The third order terms include all the first and quadratic terms and the terms  $x^3, xyz, xy^2, \ldots$ , totally 19 terms. The quadratic terms in Fig. 3 are respectively replaced by the first and third order terms to obtain the classification accuracy as shown in Fig. 8. The result shows that quadratic terms based method outperforms the other two methods. In particular, the quadratic terms have a significant performance improvement over the first order terms. The classical methods such as PointNet [1], PointNet++ [12] and DGCNN [14] all belong to the firstorder-terms based methods. This indicates that the quadratic terms are more descriptive than the traditional first order terms. This also proves that the physical implication of learning based on quadratic terms is more reasonable than that of first order terms. The learning based on first order terms can be considered as point cloud description on reference plane.

As shown in Fig. 3, our classification baseline has only one convolution layer to learn the function coefficients. Nevertheless, it has a strong ability to classify the 3D objects. Table I lists the classification accuracy of our method and the other state-of-the-art methods. The results show that the accuracy of our baseline is 89.5% on MN40, which is higher than the 89.2% of multiple-layers PointNet [1]. On MN10, our baseline achieves a accuracy of 94.0%, higher than PointNet++'s accuracy of 93.3%.

Meanwhile, the baseline is very lightweight and fast. As recorded in Table II, our baseline has approximately 0.4 M parameters, an order of magnitude lower than PointNet [1]. The flops of our baseline for one sample is 3.2 M, two orders

 TABLE I

 3D object classification result (%) on ModelNet40 (MN40) and

 ModelNet10 (MN10). The best ones are marked in red, and the

 second best ones are in blue ("-": unknown).

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Method	points	MN40	MN10
Pointwise-CNN [45]	1k	86.0	-
Deep Sets [46]	1k	87.1	-
ECC [47]	1k	87.4	90.0
PointNet [1]	1k	89.2	91.9
<b>Baseline</b> (Ours)	1k	89.5	94.0
SCN [48]	1k	90.0	-
Flex-Conv [49]	1k	90.2	-
Kd-Net(depth=10) [50]	1k	90.6	-
PointNet++ [12]	1k	90.7	93.3
KCNet [51]	1k	91.0	94.4
MRTNet [52]	1k	91.2	-
Spec-GCN [53]	1k	91.5	-
PointCNN [54]	1k	91.7	-
PCNN [55]	1k	92.3	-
RSCNN (single-scale) [3]	1k	92.3	94.2
RSCNN+PA [56]	1k	92.7	96.0
KPConv [57]	1k	92.7	-
<b>RSCNN+PS</b> (Ours)	1k	92.9	96.1
PointASNL [58]	1k	92.9	95.7
DGCNN [14]	1k	92.9	94.8
DensePoint [59]	1k	32.2	96.6
DGCNN+PA [56]	1k	93.4	96.7
DGCNN+PS (Ours)	1k	93.5	96.4
SO-Net [22]	2k	90.9	94.1
PointNet++ [12]	5k	91.9	-
SpiderCNN [60]	5k	92.4	-
DGCNN [14]	2k	93.5	95.5
DGCNN+PS (Ours)	2k	94.2	96.5

 TABLE II

 THE COMPARISON OF COMPLEXITY OF DIFFERENT METHODS.

Method	params	FLOPs/sample
PointNet [1]	3.5 M	440 M
PointNet++ [12]	1.48 M	1684 M
Baseline	0.4 M	3.2 M
DGCNN+PS	1.818 M	2586 M
DGCNN [14]	1.813 M	2484 M
PS	4992	102 M

of magnitude lower than PointNet [1] and approximately 0.2% of PointNet++ [12]. Therefore, this baseline is suitable for massive point clouds or a low computing power device. With regard to our PS module, we use DGCNN [14] network to calculate the additional parameters and flops. As shown in Table II, the original DGCNN has 1.813 M parameters and 2484 M flops. After adding our PS module, the increase is 4992 and 102 M, respectively, which is an increase of 0.28% and 4.11% over the original DGCNN. This indicates that our PS module also has lower calculation cost.

2) 3D Classification: To further verify the effectiveness of our method, we expand the baseline with DGCNN [14] (Fig. 5) and RSCNN [3] (Fig. 6) networks for classification. We compare our method with the state-of-the-art methods on MN40 and MN10 datasets. Table I shows the classification accuracy of popular methods and the modified versions equipped with our representation. As shown in Table I, compared with

This article has been accepted for publication in a future issue of this journal, but has not been fully edited. Content may change prior to final publication. Citation information: DOI 10.1109/TCSVT.2021.3095233, IEEE Transactions on Circuits and Systems for Video Technology

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TABLE III THE COMPARISON RESULT (%) OF SHAPE SEGMENTATION ON SHAPENET [42]. BEST ONES ARE MARKED IN RED, AND THE SECOND BEST ONES ARE IN BLUE.DGCNN-T: SPATIAL TRANSFORM IS REMOVED FROM DGCNN [14]

Method	class	instance	air	bag	cap	car	chair	ear	onita	r knife	lamp	lanto	nmoto	r miio	nisto	rocke	tskate	table
method	mIoU	mIoU	plane	0	eup	cui	enun	phone	•	i kinite	nump	Iuptoj	bike	mag	pistor	Toene	board	
Kd-Net [50]	77.4	82.3	80.1	74.6	74.3	70.3	88.6	73.5	90.2	87.2	81.0	94.9	57.4	86.7	78.1	51.8	69.9	80.3
PointNet [1]	80.4	83.7	83.4	78.7	82.5	74.9	89.6	73.0	91.5	85.9	80.8	95.3	65.2	93.0	81.2	57.9	72.8	80.6
RS-Net [61]	81.4	84.9	82.7	86.4	84.1	78.2	90.4	69.3	91.4	87.0	83.5	95.4	66.0	92.6	81.8	56.1	75.8	82.2
SCN [48]	81.8	84.6	83.8	80.8	83.5	79.3	90.5	69.8	91.7	86.5	82.9	96.0	69.2	93.8	82.5	62.9	74.4	80.8
PCNN [55]	81.8	85.1	82.4	80.1	85.5	79.5	90.8	73.2	91.3	86.0	85.0	95.7	73.2	94.8	83.3	51.0	75.0	81.8
SPLATNet [62]	82.0	84.6	81.9	83.9	88.6	79.5	90.1	73.5	91.3	84.7	84.5	96.3	69.7	95.0	81.7	59.2	70.4	81.3
KCNet [51]	82.2	84.7	82.8	81.5	86.4	77.6	90.3	76.8	91.0	87.2	84.5	95.5	69.2	94.4	81.6	60.1	75.2	81.3
PointASNL [58]	83.4	86.1	84.1	84.7	87.9	79.7	92.2	73.7	91.0	87.2	84.2	95.8	74.4	95.2	81.0	63.0	76.3	83.2
KPConv [57]	85.1	86.4	84.6	86.3	87.2	81.1	91.1	77.8	92.6	88.4	82.7	96.2	78.1	95.8	85.4	69.0	82.0	83.6
DensePoint [59]	84.2	86.4	84.0	85.4	90.0	79.2	91.1	81.6	91.5	87.5	84.7	95.9	74.3	94.6	82.9	64.6	76.8	83.7
DGCNN [14]	82.3	85.2	84.0	83.4	86.7	77.8	90.6	74.7	91.2	87.5	82.8	95.7	66.3	94.9	81.1	63.5	74.5	82.6
DGCNN+PS	80.9	85.5	80.9	81.9	88.0	81.3	90.7	68.2	91.7	87.1	84.9	91.6	64.0	93.7	78.0	53.3	74.2	84.6
DGCNN-T	80.0	85.1	82.1	77.9	80.3	77.2	90.9	73.6	90.9	88.5	85.2	95.6	56.2	93.8	78.4	50.4	74.6	83.5
DGCNN-T+PS	80.7	85.4	81.0	84.9	94.5	83.6	90.1	56.6	91.6	87.4	83.3	96.4	67.7	91.8	74.1	56.2	68.0	84.4
RSCNN [3]	84.0	86.2	83.5	84.8	88.8	79.6	91.2	81.1	91.6	88.4	86.0	96.0	73.7	94.1	83.4	65.5	77.7	83.6
RSCNN+PS	84.5	86.5	84.3	84.5	95.5	82.2	91.0	68.5	90.6	83.4	85.7	91.7	77.5	94.7	85.3	73.3	79.7	84.7

RSCNN [3], our representation improves the accuracy by 0.6%and 1.9% on MN40 and MN10, respectively, higher than that of PointAugment (PA) [56]. On the basis of the performance of DGCNN [14], our method improves by 0.6% and 1.6% on MN40 and MN10, respectively, outperforming the other methods on MN40. The improvement is close to that of PA [56]. When the input number of points is 2 k, our method has an accuracy of 94.2% on MN40 and 96.5% on MN10, superior to the state-of-the-art methods on both datasets. Compared with other methods, our performance improvement is significant. These results indicate that the point-to-surface representation plays a significant and positive role in improving the accuracy of 3D classification.

3) Shape Part Segmentation: In order to verify the effectiveness of our PS module on point cloud segmentation, we also modify the DGCNN [14] and RSCNN [3] networks with our representation for comparison. The modified DGCNN is shown in Fig. 5. The modified RSCNN is shown in Fig. 7. We use the popular ShapeNet part benchmark [42] to evaluate our method and the state-of-the-art methods. Referring to [3], the number of the input points is 2,048. The methods are evaluated by mean Inter-over-Union (mIoU). Table III records the mean IoU, class IoU and every category IoU of different methods.

When we directly add the PS module into the DGCNN [14], the results in Table III show that the instance mIoU increases by 0.3% but the class mIoU decreases by 1.4%. One possible reason is that the spatial transformation of DGCNN [14] changes the original Euclidean space, causing the proposed representation meaningless. In order to verify this point, we remove the spatial transformation from the above comparative experiments, so that the coordinates are in Euclidean space. In Table III, the two experiments are denoted by DGCNN-T+PS and DGCNN-T, respectively. The results show that the modified DGCNN improves the class mIoU and instance mIoU by 0.7% and 0.3%, respectively, which is significant. This result indicates that our PS module is effective for

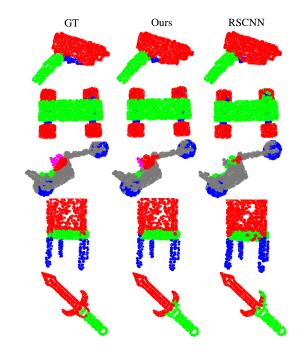


Fig. 9. The comparison of segmentation results between our method and RSCNN [3]. Different colors represent the segmentation results of different parts.

the traditional Euclidean spatial point cloud but not for the transformed non-Euclidean space. For the traditional networks based on Euclidean coordinates, such as RSCNN [3], after embedding our PS module, the class mIoU and instance mIoU are 84.5% and 86.5%, respectively. The instance mIoU is superior to the other methods. Compared with RSCNN [3], our method improves the class and instance mIoU by 0.5% and 0.3%, respectively. Meanwhile, our method outperforms the others on multiple objects part segmentation as shown in Table III. In particular, the results also show that the performance of air plane, cap, car, motor bike, pistol, rocket,

TABLE IV The comparison results of the semantic segmentation on ScanNet dataset between the FPConv [44] and the modified network with our PS module. The results include segmentation mIoU, mean class accuracy (mA) and over all class accuracy (oA) (%).

Model	mIoU	mA	oA
FPConv [44]	62.2	74.3	84.6
FPConv+PS	62.6	75.6	84.6

skateboard and table is improved significantly by using our PS module. We also compare some segmentation results with RSCNN [3] as shown in Fig. 9. These results show that our method has better result for small parts segmentation. More results are in Appendix A. The above experimental results indicate that our point-to-surface representation can enhance the ability of network feature description in segmentation.

4) Semantic Segmentation: We also investigate the ability of the proposed point-to-surface representation for complex scenarios such as the semantic segmentation benchmark Scan-Net [43]. For the comparison, we add the PS module to the network structure of FPConv [44] as the method of the modified RSCNN. The setting for the comparison experiments are the same except for the PS module. The quantitative results are recorded in Table IV. The results show that our PS module improves the mIoU and mean class accuracy of FPConv by 0.4% and 1.3%, respectively. This means that the point-tosurface representation is also suitable for feature extraction in complex scenario.

#### C. Ablation Study

In this section, our method is analyzed by ablation study in the application of 3D classification. The ablation study is performed on the network structure of DGCNN [14]. The results are recorded in Table V. The original DGCNN has an accuracy of 92.9%. After embedding our initial point-tosurface representation without adaptive contribution weighting, the accuracy is 93.1%, improved by 0.2%. When we add the adaptive contribution weighting to DGCNN, the accuracy is improved by another 0.4%. Finally, in order to study the impact of the number of input points on performance, we increase the number of input points to 2 k for comparison. The accuracy has improved significantly, reaching 94.2%.

TABLE V
The accuracy (%) of 3D classification on $MN40$ with initial
POINT-TO-SURFACE REPRESENTATION (INIT.), ADAPTIVE CONTRIBUTION
WEIGHTING (ACW)

and number of points with DGCNN [14] network structure. MPOINTS denotes experiments with 2,048 points.

Model	INIT.	ACW	MPOINTS	Acc.
DGCNN [14]				92.9
DGCNN+	$\checkmark$			93.1
DGCNN+	$\checkmark$	$\checkmark$		93.5
DGCNN+	$\checkmark$	$\checkmark$	$\checkmark$	94.2

We also analyze the effect of the surface function number on performance. Fig. 10 shows the comparison results with different surface function number in baseline. The experimental results indicate that increasing the number of surface functions can improve the ability of shape representation. As the number of functions increases to a certain extent, the improvement gradually flattens out. Therefore, a better performance does not require a large number of parameters and computation.

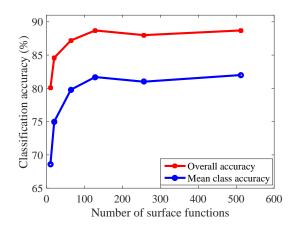


Fig. 10. Results of our baseline with different numbers of surface functions.

Finally, we test the robustness of the point-to-surface representation to the number of the input points. We trained our model with 64, 128, 256, 512, 1, 024 and 2, 048 points, respectively. The test classification accuracy is shown in Fig. 11. The result shows that our method is robust for different number of input points. Even with 64 input points, the model still keeps a higher classification ability. This is of great significance for the lightweight and real-time applications.

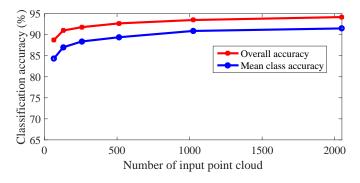


Fig. 11. Results of classification trained by 64, 128, 256, 512, 1,024 and 2,048 points with our method.

## D. Visualization

1) Learned Reference Surfaces: In the training step, we learn the underlying surfaces through unsupervised learning. In order to visualize these underlying surfaces, we first utilize the learned surface function coefficients to get the shape point cloud by giving the x and y coordinates and solving the z coordinate. The mesh surface is reconstructed by transforming the point cloud to meshes with MeshLab [63] software. Some reconstructed surfaces are shown in Fig. 12. These surfaces are not obtained by fitting certain shapes, but are learned during the task to represent all 3D shapes. Since there are quadratic

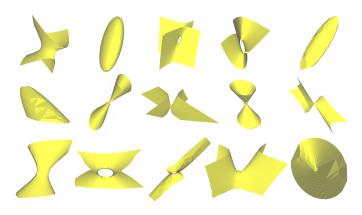


Fig. 12. Some learned surfaces with ModelNet40 benchmark. According to the surface function equation, the sampling point cloud can be obtained by giving x and y coordinates and solving the z coordinate. Then, the point cloud is used for mesh reconstruction with MeshLab [63] software.

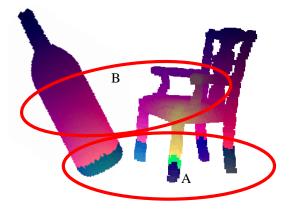


Fig. 13. Contribution visualization of a certain reference surface function. Region B shows the continuity of the surface function. Region A illustrates that different surface functions contribute differently to different parts of a 3D shape.

terms in the surface function, these surfaces are symmetric. Moreover, they differ from each other in structure, which ensure a strong representation capability.

2) Point-to-Surface Representation: Here, we want to visualize the contribution of a certain surface function to the point cloud. To this end, we set the R, G, B values of the point cloud to three surface function values. Then, we can visualize the contribution of 3 surface functions at a time. For example, in order to visualize the representation of function  $f_1(x, y, z), f_2(x, y, z), f_3(x, y, z)$ , the color of the point cloud **P** are defined as:

$$R = f_1(\mathbf{P}),$$
  

$$G = \tilde{f}_2(\mathbf{P}),$$
  

$$B = \tilde{f}_3(\mathbf{P}),$$
  
(5)

where the notation  $f_i$  denotes the normalized value. Then, all representation values are visualized by a group of colorized point cloud. Fig. 13 gives two visualization examples. As shown in Fig. 13, the circled *B* region is overly flat in colour, indicating that the output values of these surface functions are continuous at these regions. We also notice some discontinuous regions, such as the green part on the chair leg in region *A*. One possible reason is due to the ReLU activation

during the learning. Another reason is that the training makes different surface functions contribute differently to different parts of a 3D shape in a task. More point-to-surface representations are shown in Appendix B. This visualization is nontrivial for understanding and analyzing the point-to-surface representation.

# V. CONCLUSION

In this paper, a quadratic terms based point-to-surface representation has been proposed to transform the point coordinates to the relationship between the local point and the global surfaces. The static representation can also become dynamic by adaptive contribution weighting. The proposed PS module can be inserted to the existing 3D learning networks. The experimental results show that the learning based on quadratic terms is more descriptive than the first order terms. The proposed point-to-surface representation is easy to implement and lightweight. Meanwhile, the modified networks with our representation outperform the state-of-the-art methods on 3D classification and segmentation. The experimental results also indicate that the representation is robust to sparse point cloud classification.

In the future, we will focus on the rotation invariance of the point-to-surface representation. In addition, the problem of over-fitting in 3D vision tasks is another problem worthy of further study.

# APPENDIX A PART SEGMENTATION RESULTS

More part segmentation results are displayed in Fig. 14. We compare the results of our method with the Ground Truth (GT). Please zoom-in for clearer visualization.

# APPENDIX B THE VISUALIZATION OF THE POINT TO SURFACE REPRESENTATION

More surface function representations are shown in Fig. 15. As we can only visualize 3 functions at a time by setting RGB values. Hence, we visualize the contributions of 63 surface functions by 21 point clouds for one shape. In Fig. 15, these 21 point clouds are divided into 3 rows, with 7 columns in each row. The row number is indexed by i, the column number is indexed by j, the color of different point cloud represents different surface function as follows:

$$R = \tilde{f}_{21 \times j + 3 \times i}(\mathbf{P}),$$
  

$$G = \tilde{f}_{21 \times j + 3 \times i + 1}(\mathbf{P}),$$
  

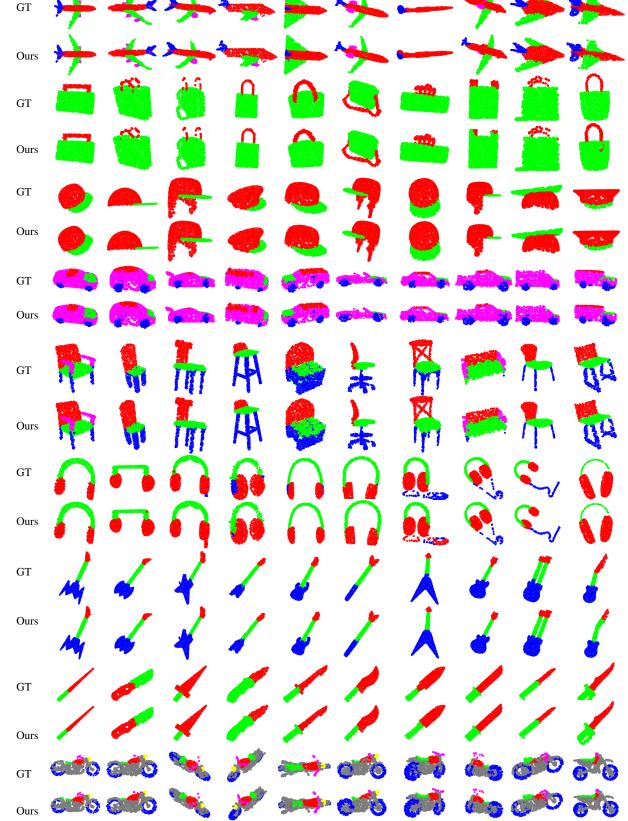
$$B = \tilde{f}_{21 \times j + 3 \times i + 2}(\mathbf{P}).$$
(6)

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Fig. 14. More part segmentation results on ShapeNet dataset. The results are obtained by the modified RSCNN with our PS module.



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*i* = 3

i = 4

*i* = 5

*i* = 6

*i* = 2

 $\begin{array}{l} \mathbf{R} = \tilde{f}_{21 \times j + 3 \times i} \left( \mathbf{P} \right) \\ \mathbf{G} = \tilde{f}_{21 \times j + 3 \times i + 1} \left( \mathbf{P} \right) \\ \mathbf{B} = \tilde{f}_{21 \times j + 3 \times i + 2} \left( \mathbf{P} \right) \end{array}$ 

j = 0

j = 1

j=2

j = 0

j = 1

j = 2

j = 0

i = 0

*i* = 1

i = 1j = 2影 卧 北 j = 0j = 1j = 2j = 0j = 1j = 2Fig. 15. The visualization of point-to-surface representation. The three channels R, G and B of the point cloud color respectively represent the normalized functional values of the point cloud to three reference surfaces. For each shape, we have visualized  $3 \times 3 \times 7 = 63$  point-to-surface representations. 1051-8215 (c) 2021 IEEE. Personal use is permitted, but republication/redistribution reguires IEEE permission. See http://www.ieee.org/publications\_standards/publications/rights/index.html for more information. Authorized licensed use limited to: University of Electronic Science and Tech of China. Downloaded on December 15,2021 at 05:12:15 UTC from IEEE Xplore. Restrictions apply.

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